Jiating Yu, Jiacheng Leng, Fan Yuan, Duanchen Sun, Ling-Yun Wu

Academy of Mathematics and Systems Science, Chinese Academy of Sciences, Beijing, China

Presented by: Yijingxiu Lu

Jiating Yu, Jiacheng Leng, Fan Yuan, Duanchen Sun, Ling-Yun Wu

Academy of Mathematics and Systems Science, Chinese Academy of Sciences, Beijing, China

**≠** Generative Diffusion

#### **One-Sentence Summary:**

٠

- Denoise gene regulatory network with the reversed diffusion process defined by random walk on graph.
  - diffusion process defined by random walk on graph: proposed as Network Refinement (Yu et al. 2023)

$$b\left(\frac{f_m}{g(W)}\right)$$

• reversed diffusion process defined by random walk on graph:

$$b\left(f_m^{-1}(g(W))\right)$$

Task: Denoise gene regulatory network

- **Input:** noisy observed network G<sub>obs</sub>
- **Output:** direct network G<sub>dir</sub>

**Method:** REverse Network Diffusion On Random walks (RENDOR) (Network Diffusion  $\neq$  Generative Diffusion)

**Benchmark:** Dialogue on Reverse Engineering Assessment and Methods (DREAM)

- DREAM provides high-confidence networks for *E. coli* and *S. aureus*, each comprising ~1,700 transcriptional interactions at a precision of ~50%.
  - **<u>E.coli</u>**: experimentally validated interactions from a curated database (RegulonDB<sup>16</sup>)
  - **<u>ChIP-chip:</u>** a high-confidence set of interactions supported by genome-wide transcription-factor binding data
  - <u>S. cerevisiae</u>: evolutionarily conserved binding motifs
  - in silico data

#### **One-Sentence Summary:**

٠

- Denoise gene regulatory network with the reversed diffusion process defined by random walk on graph.
  - diffusion process defined by random walk on graph: proposed as Network Refinement (Yu et al. 2023)

$$b(f_m(g(W)))$$

• reversed diffusion process defined by random walk on graph:

$$h\big(f_m^{-1}\big(g(W)\big)\big)$$

Task: Denoise gene regulatory network

- **Input:** noisy observed network G<sub>obs</sub>
- **Output:** direct network G<sub>dir</sub>

#### Network Diffusion

• Describe the movement process of entities or states in the network

#### Generative Diffusion

Uses diffusion and denoising processes
 to generate high-quality data

**Method:** REverse Network Diffusion On Random walks (RENDOR) (Network Diffusion  $\neq$  Generative Diffusion)

**Benchmark:** Dialogue on Reverse Engineering Assessment and Methods (DREAM)

- DREAM provides high-confidence networks for *E. coli* and *S. aureus*, each comprising ~1,700 transcriptional interactions at a precision of ~50%.
  - **<u>E.coli</u>**: experimentally validated interactions from a curated database (RegulonDB<sup>16</sup>)
  - **<u>ChIP-chip:</u>** a high-confidence set of interactions supported by genome-wide transcription-factor binding data
  - <u>S. cerevisiae</u>: evolutionarily conserved binding motifs
  - in silico data

## Framework



Transitive Closure (TC)





Transitive Closure (TC)











# Network Refinement (NR) Yu et al. 2023

**<u>Goal</u>**: Enhance signals in network





# Network Refinement: Denoising complex networks for better community detection



Jiating Yu<sup>a,b</sup>, Jiacheng Leng<sup>a,b</sup>, Duanchen Sun<sup>c</sup>, Ling-Yun Wu<sup>a,b,\*</sup>

<sup>a</sup> IAM, MADIS, NCMIS, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, Beijing 100190, China <sup>b</sup> School of Mathematical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China <sup>c</sup> School of Mathematics, Shandong University, Jinan, Shandong 250100, China

#### Summary

#### Background

#### **Related Works**

#### Methodology

#### Main Results

Contents lists available at ScienceDirect

Physica A

journal homepage: www.elsevier.com/locate/physa

A.A. DESCRIPTION A.D. DESCRIPTION A.D. DESCRIPTION

# Network Refinement (NR) Yu et al. 2023

<u>Goal:</u> Enhance signals in network <u>Method:</u> global network diffusion process defined by random walk on graph



**RENDOR** =

 $b(f_m^{-1}(g(W)))$ 

Pseudocode for RENDOR

Input: W<sub>obs</sub>: weighted adjacency matrix of observed network; m: diffusion intensity parameter;

 $\varepsilon_1, \varepsilon_2$ : preprocessing parameters.

Output:  $W_{dir}$ : denoised adjacency matrix of direct network.

1. 
$$\tilde{W}_{obs} = W_{obs} + \varepsilon_1 J + \varepsilon_2 I$$
  
2.  $P_{obs} = g(\tilde{W}_{obs}) = (diag\{\tilde{W}_{obs}1\})^{-1} \tilde{W}_{obs}$   
3.  $P_{dir} = f_m^{-1}(P_{obs}) = m((m-1)I + P_{obs})^{-1}P_{obs}$   
4. for  $i = 1, ..., n$ :  
if  $\min_j\{(P_{dir})_{ij}\} \ge 0$ :  $\beta_i = 0$   
else:  $\beta_i = \min_j\{(P_{dir})_{ij}\}$   
5.  $\tilde{P}_{dir} = P_{dir} - (\beta_1 1, ..., \beta_n 1)^T$   
6.  $W_{dir} = b(\tilde{P}_{dir}) = diag\{\pi(\tilde{P}_{dir})\}\tilde{P}_{dir}$ 

**RENDOR** =

 $b(f_m^{-1}(g(W)))$ 

Pseudocode for RENDOR

Input: W<sub>obs</sub>: weighted adjacency matrix of observed network; m: diffusion intensity parameter;

 $\varepsilon_1, \varepsilon_2$ : preprocessing parameters.

Output:  $W_{dir}$ : denoised adjacency matrix of direct network.

1.  $\tilde{W}_{obs} = W_{obs} + \varepsilon_1 J + \varepsilon_2 I$  Ensure that the input matrix mat is symmetric and normalized 2.  $P_{obs} = g(\tilde{W}_{obs}) = (diag\{\tilde{W}_{obs}1\})^{-1}\tilde{W}_{obs}$ 3.  $P_{dir} = f_m^{-1}(P_{obs}) = m((m-1)I + P_{obs})^{-1}P_{obs}$ 4. for i = 1, ..., n: if  $\min_j\{(P_{dir})_{ij}\} \ge 0$ :  $\beta_i = 0$ else:  $\beta_i = \min_j\{(P_{dir})_{ij}\}$ 5.  $\tilde{P}_{dir} = P_{dir} - (\beta_1 1, ..., \beta_n 1)^T$ 6.  $W_{dir} = h(\tilde{P}_{dir}) = diag\{\pi(\tilde{P}_{dir})\}\tilde{P}_{dir}$ 

**RENDOR** =

 $b\bigl(f_m^{-1}\bigl(g(W)\bigr)\bigr)$ 

Pseudocode for RENDOR

Input: W<sub>obs</sub>: weighted adjacency matrix of observed network; m: diffusion intensity parameter;

 $\varepsilon_1, \varepsilon_2$ : preprocessing parameters.

Output:  $W_{dir}$ : denoised adjacency matrix of direct network.

1.  $\tilde{W}_{obs} = W_{obs} + \varepsilon_1 J + \varepsilon_2 I$  Ensure that the input matrix mat is symmetric and normalized 2.  $P_{obs} = g(\tilde{W}_{obs}) = (diag\{\tilde{W}_{obs}1\})^{-1} \tilde{W}_{obs}$   $g(W) = D^{-1}W$ 3.  $P_{dir} = f_m^{-1}(P_{obs}) = m((m-1)I + P_{obs})^{-1}P_{obs}$ 4. for i = 1, ..., n: if  $\min_j\{(P_{dir})_{ij}\} \ge 0$ :  $\beta_i = 0$ else:  $\beta_i = \min_j\{(P_{dir})_{ij}\}$ 5.  $\tilde{P}_{dir} = P_{dir} - (\beta_1 1, ..., \beta_n 1)^T$ 6.  $W_{dir} = b(\tilde{P}_{dir}) = diag\{\pi(\tilde{P}_{dir})\}\tilde{P}_{dir}$ 

**RENDOR** =

 $b(f_m^{-1}(g(W)))$ 

Pseudocode for RENDOR

Input: W<sub>obs</sub>: weighted adjacency matrix of observed network; m: diffusion intensity parameter;

 $\varepsilon_1, \varepsilon_2$ : preprocessing parameters.

Output:  $W_{dir}$ : denoised adjacency matrix of direct network.

1.  $\tilde{W}_{obs} = W_{obs} + \varepsilon_1 J + \varepsilon_2 I$  Ensure that the input matrix mat is symmetric and normalized 2.  $P_{obs} = g(\tilde{W}_{obs}) = (diag\{\tilde{W}_{obs}1\})^{-1} \tilde{W}_{obs}$   $g(W) = D^{-1}W$ 3.  $P_{dir} = f_m^{-1}(P_{obs}) = m((m-1)I + P_{obs})^{-1}P_{obs}$   $f_m^{-1}(P) = m((m-1)I + P)^{-1}P$ 4. for i = 1, ..., n: if  $\min_j\{(P_{dir})_{ij}\} \ge 0$ :  $\beta_i = 0$ else:  $\beta_i = \min_j\{(P_{dir})_{ij}\}$ 5.  $\tilde{P}_{dir} = P_{dir} - (\beta_1 1, ..., \beta_n 1)^T$ 6.  $W_{dir} = b(\tilde{P}_{dir}) = diag\{\pi(\tilde{P}_{dir})\}\tilde{P}_{dir}$ 

**RENDOR** =

 $b(f_m^{-1}(g(W)))$ 

Pseudocode for RENDOR

Input: W<sub>obs</sub>: weighted adjacency matrix of observed network; m: diffusion intensity parameter;

 $\varepsilon_1, \varepsilon_2$ : preprocessing parameters.

Output:  $W_{dir}$ : denoised adjacency matrix of direct network.

1.  $\tilde{W}_{obs} = W_{obs} + \varepsilon_1 J + \varepsilon_2 I$  Ensure that the input matrix mat is symmetric and normalized 2.  $P_{obs} = g(\tilde{W}_{obs}) = (diag\{\tilde{W}_{obs}1\})^{-1}\tilde{W}_{obs}$   $g(W) = D^{-1}W$ 3.  $P_{dir} = f_m^{-1}(P_{obs}) = m((m-1)I + P_{obs})^{-1}P_{obs}$   $f_m^{-1}(P) = m((m-1)I + P)^{-1}P$ 4. for i = 1, ..., n: if  $\min_j\{(P_{dir})_{ij}\} \ge 0$ :  $\beta_i = 0$ else:  $\beta_i = \min_j\{(P_{dir})_{ij}\}$ 5.  $\tilde{P}_{dir} = P_{dir} - (\beta_1 1, ..., \beta_n 1)^T$ 6.  $W_{dir} = b(\tilde{P}_{dir}) = diag\{\pi(\tilde{P}_{dir})\}\tilde{P}_{dir}$   $b(P) = \alpha \cdot diag(\pi(P))$ 

# Methodology (code from github)

```
function [output network]=RNDRW(mat, m)
 1
 2
      [n_tf,n]=size(mat);
 3
      for i=1:n tf
 4
          mat(i,i)=0;
 5
      end
 6
 7
 8
      9
      mat(1:n_tf,1:n_tf)=(mat(1:n_tf,1:n_tf)+mat(1:n_tf,1:n_tf)')/2;
10
      mat1=[mat;[zeros(n-n tf,n tf),eye(n-n tf,n-n tf)]];
11
      mat1=(mat1+mat1')/2;
12
13
      mat1=(mat1-min(mat1(:)))/(max(mat1(:))-min(mat1(:)));
      mat1=mat1+min(mat1(mat1>0))+min(mat1(mat1>0))*eye(n);
14
15
16
      % mat1=[mat;[mat(:,(n tf+1):end)',eye(n-n tf,n-n tf)]];
17
18
      % mat1=(mat1+mat1')/2;
      % mat1=(mat1-min(mat1(:)))./(max(mat1(:))-min(mat1(:)));
19
      % mat1=mat1+min(mat1(mat1>0));
20
```

21	
22	
23	%% ***********************************
24	<pre>P1 = mat1./sum(mat1,2);</pre>
25	P2 = m * P1 /((m-1)*eye(n) + P1);
26	P2 = P2 - min(min(transpose(P2)),0)';
27	P2 = P2 ./ sum(P2,2);
28	<pre>stat_d = abs(null((P2-eye(n))'));</pre>
29	<pre>net_new = diag(stat_d)*P2;</pre>
30	
31	
32	<b>%</b> ************************************
33	<pre>net_new = net_new + net_new';</pre>
34	<pre>output_network = net_new(1:n_tf, :);</pre>

### Experiments

on the simulated networks

We compared the denoising performance of RENDOR with four other state-of-the-art GRN denoising methods: ND (Feizi *et al.* 2013), NE (Wang *et al.* 2018), Silencer (Barzel and Barabási 2013), and inverse correlation matrix (ICM) (Alipanahi and Frey 2013).



### Experiments

on DREAM5 dataset

We compared the denoising performance of RENDOR with four other state-of-the-art GRN denoising methods: ND (Feizi *et al.* 2013), NE (Wang *et al.* 2018), Silencer (Barzel and Barabási 2013), and inverse correlation matrix (ICM) (Alipanahi and Frey 2013).



## Conclusion

- In this work, authors propose RENDOR, a novel denoising approach for improving the accuracy of network inference.
- RENDOR is designed to handle noisy networks affected by indirect effects.
  - effectively models higher-order indirect interactions between nodes through network diffusion, employs reverse network diffusion to <u>eliminate indirect effects</u>, and outputs refined networks containing only direct signal edges.
- Through comprehensive evaluations on both **simulated noisy networks** and **real GRNs**, the authors demonstrated that RENDOR consistently outperforms alternative denoising methods for GRN inference, enhancing the inference accuracy by effectively mitigating the impact of indirect noise.